

# 紀伊水道における海洋短波レーダーを 利用した津波早期警報

Tsunami early warning using high-frequency ocean radar system  
in the Kii Channel, Japan

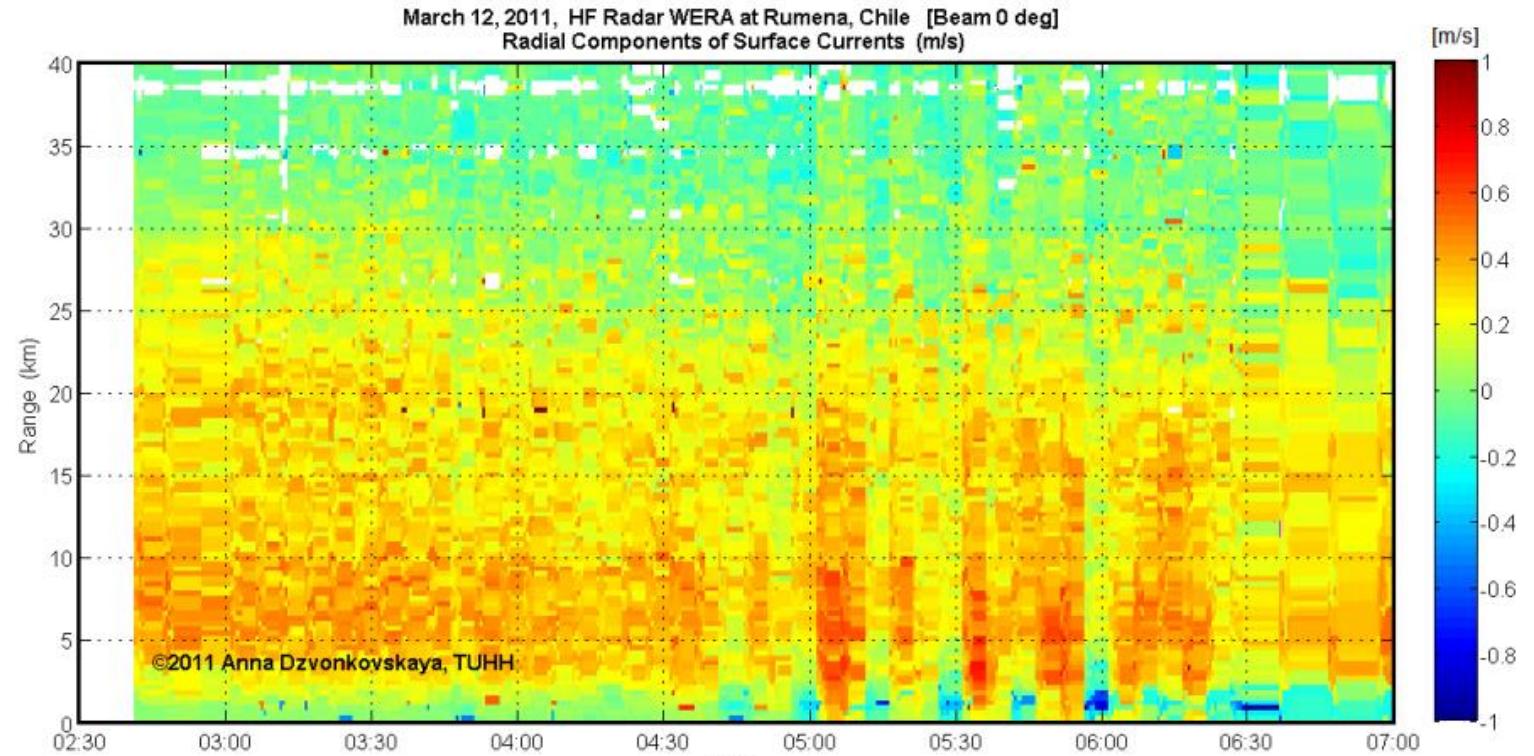
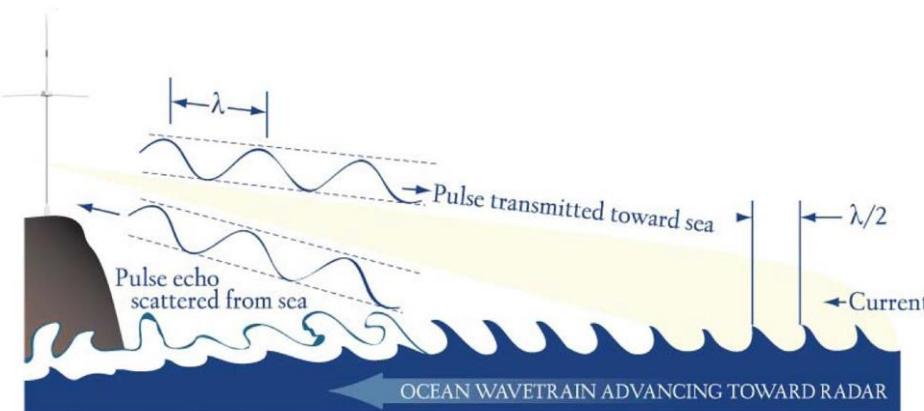
王宇晨, 今井健太郎, 堀川博紀

国立研究開発法人海洋研究開発機構

# 1. はじめに

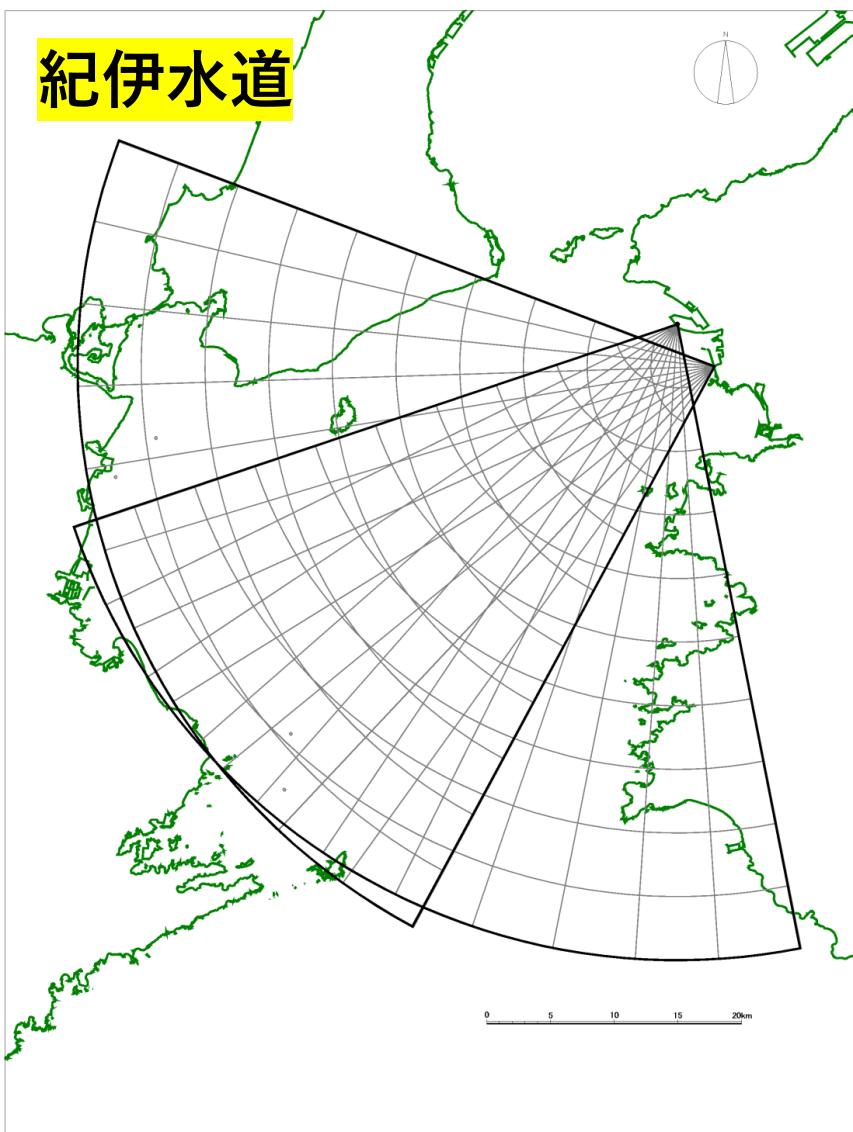
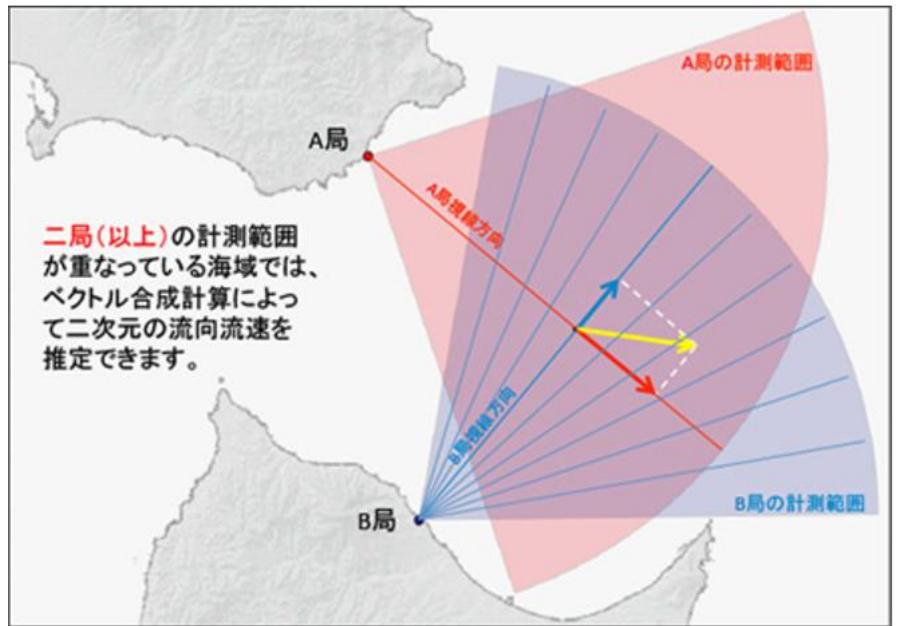
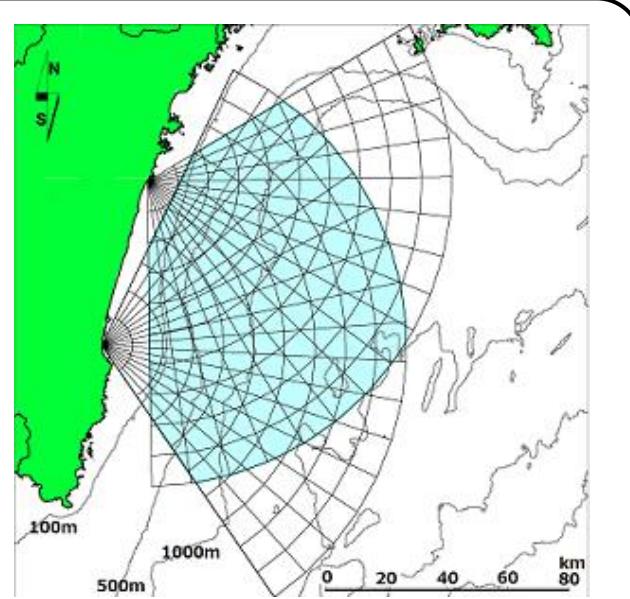
## High-frequency (HF) ocean radar

Example: HF radar in Chile observed the tsunami of the 2011 Tohoku earthquake.



(Dzvonkovskaya et al., 2011; Roarty et al., 2019)

# HF radar in Japan



(Figure Source: JAMSTEC, MLIT, Miyazaki Prefecture)

## 2. データ解析

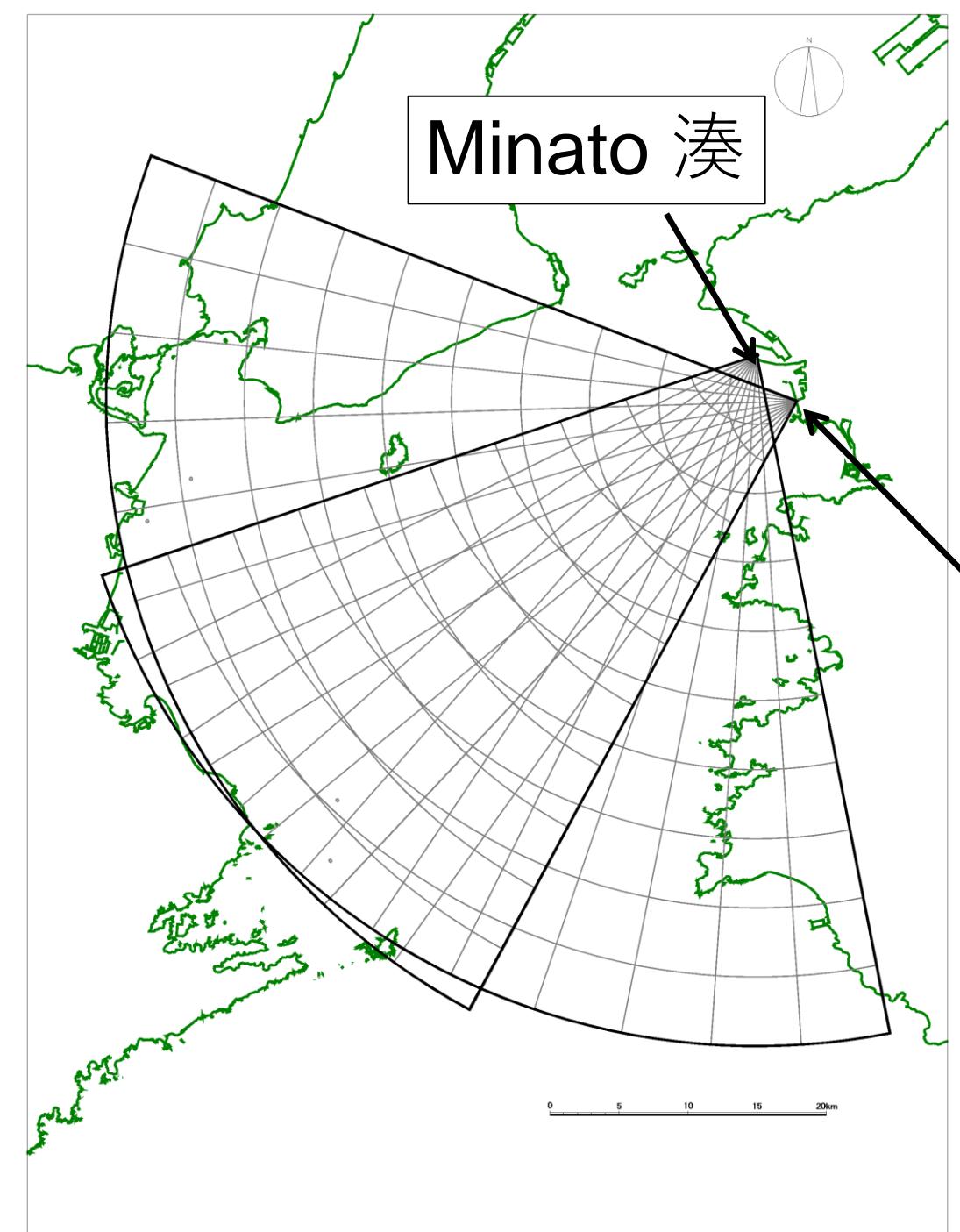
### 2011 Tohoku Tsunami

- Generated by the M9 Tohoku Earthquake on March 11, 2011
- Arrived in Kii Channel approximately 3 hours after the earthquake



(Figure Source: The New York Times)





	1.5km	3.0km	4.5km	6.0km	7.5km	9.0km	10.5km	12.0km	13.5km	15.0km	16.5km	18.0km	19.5km
1	2011/03/11 17:00	-15.1957	-15.1844	-15.8271	-17.7073	-19.4555	-21.4676	-22.8103	-24.6966	-26.5829	-28.4693	-29.6476	-29.8905
2	2011/03/11 17:01	-15.6833	-14.8651	-15.8156	-17.6778	-18.9530	-20.1125	-21.7173	-25.4116	-27.6959	-31.0670	-30.0643	-29.2721
3	2011/03/11 17:02	-10.3371	-13.3751	-15.1622	-18.5458	-20.1113	-20.9373	-22.3357	-23.7341	-25.0048	-27.0743	-28.1828	-27.9297
4	2011/03/11 17:03	-3.0582	-7.2220	-9.4127	-19.3476	-20.4926	-22.9810	-24.2169	-25.8400	-27.4631	-25.4811	-25.0441	-25.5176
5	2011/03/11 17:04	-6.2533	-5.2644	-9.3781	-13.1067	-16.8353	-20.2075	-19.7403	-20.6884	-21.6365	-23.5763	-25.8693	-26.0569
6	2011/03/11 17:05	-6.0807	-8.6887	-11.2966	-14.6631	-17.4889	-20.3107	-20.6882	-20.3267	-21.5047	-23.0069	-24.1760	-24.7751
7	2011/03/11 17:06	-6.3532	-7.9238	-10.5781	-11.1145	-13.6368	-15.5411	-17.4455	-19.3498	-20.5751	-22.3729	-23.2196	-24.0022
8	2011/03/11 17:07	-7.9812	-8.5969	-10.9609	-12.4607	-13.9641	-15.4603	-17.5421	-17.0884	-18.9078	-18.7271	-20.2987	-22.1984
9	2011/03/11 17:08	-4.8705	-4.6466	-5.7913	-12.1165	-12.4587	-14.4216	-15.2374	-16.2777	-18.2129	-19.9873	-21.5460	-22.3175
10	2011/03/11 17:09	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000
11	2011/03/11 17:10	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000
12	2011/03/11 17:11	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000
13	2011/03/11 17:12	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000
14	2011/03/11 17:13	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000
15	2011/03/11 17:14	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000	-999.9000
16	2011/03/11 17:15	-2.2316	-2.5492	-3.7429	-6.8551	-9.1880	-12.0997	-14.8446	-15.8066	-17.3740	-18.2702	-19.8265	-21.5730
17	2011/03/11 17:16	5.4540	2.6245	-1.5938	-5.9057	-8.7972	-11.9467	-14.3472	-16.2112	-17.2149	-18.2329	-19.2509	-20.6890
18	2011/03/11 17:17	2.4169	3.4239	3.008	3.5147	-7.3908	-11.6097	-13.4333	-15.6615	-16.2778	-16.4018	-18.1043	-20.3310
19	2011/03/11 17:18	-9.1403	-4.6825	-6.2843	-7.3099	-8.6186	-10.4038	-12.8934	-13.9576	-17.3986	-19.5165	-21.8225	-23.7100
20	2011/03/11 17:19	2.2718	3.9085	1.4419	-5.5000	-9.0922	-13.8697	-16.2088	-19.6118	-20.8623	-22.9264	-24.0579	-25.5399
21	2011/03/11 17:20	6.6337	3.2427	1.4884	-2.1509	-6.1525	-9.2776	-13.1280	-19.2000	-20.0161	-23.5324	-24.1892	-25.6104
22	2011/03/11 17:21	2.0699	-1.0273	-3.5583	-5.4621	-8.3431	-10.3235	-13.1279	-16.5608	-19.3355	-22.2381	-23.2439	-25.4723
23	2011/03/11 17:22	-0.0213	-1.2381	-4.7408	-7.1005	-8.9489	-11.8200	-14.3309	-17.2835	-20.0017	-22.6352	-24.4473	-26.3438
24	2011/02/11 17:22	77.62	-2.0848	-1.4924	-2.8205	-1.1122	-1.2226	-1.1222	-1.1622	-1.1022	-1.0122	-0.9220	-0.8220

観測データ @湊 (処理前)

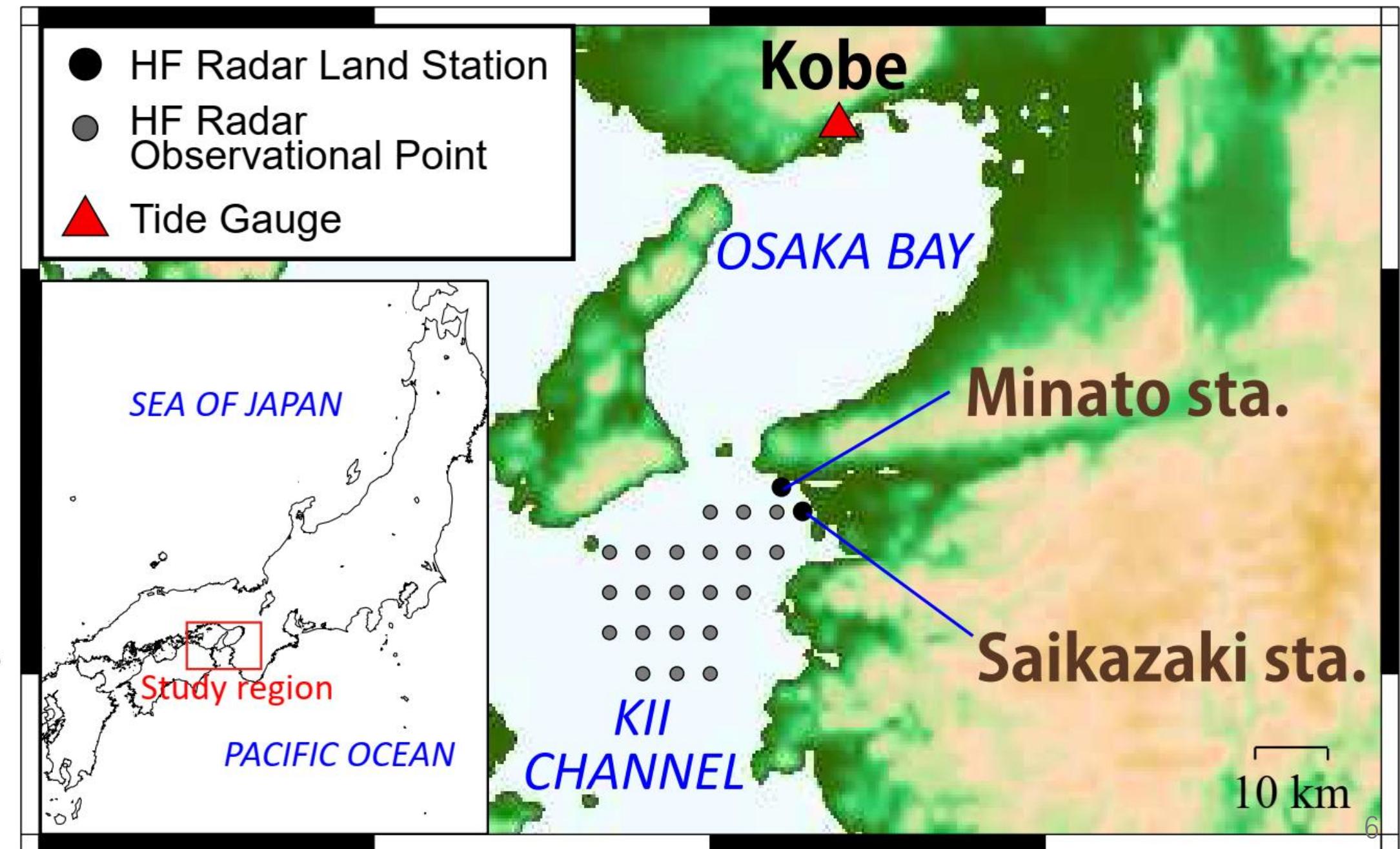
Saikazaki 雜賀崎

The tsunamis of the 2011 Tohoku earthquake was observed by high-frequency radar system in Kii Channel.  
**Sampling rate: 1 min**

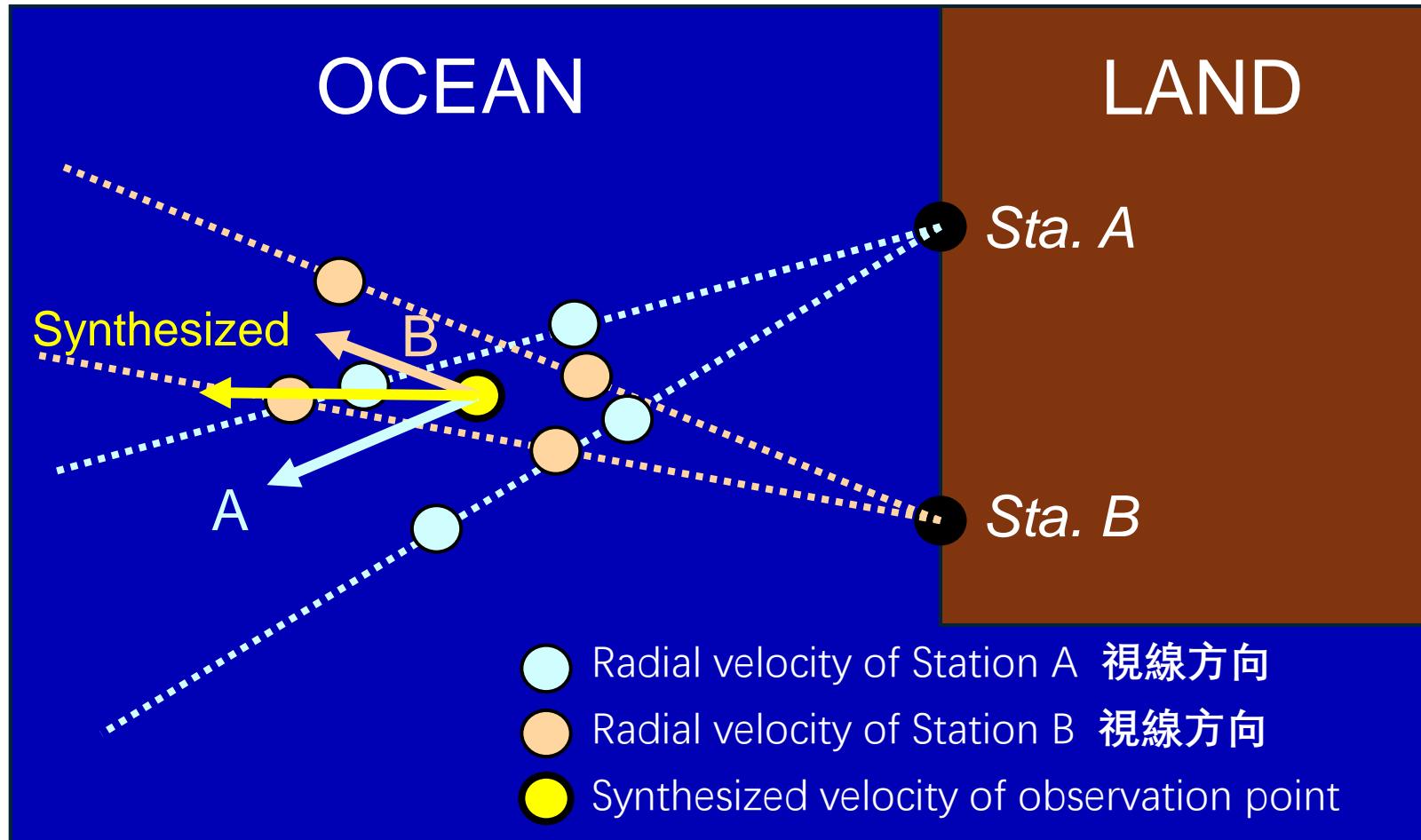
134°

135°

136°



# Vector Synthesis of Surface Vector



- At least **two** land stations are required for vector synthesis
- It is necessary to install the beams of the two stations to be close to **90 degrees**

Beam direction (radial velocity) -> NS/EW direction

# Vector Synthesis of Surface Vector

$$\begin{bmatrix} \sin\theta_1 & \cos\theta_1 \\ \sin\theta_2 & \cos\theta_2 \\ \vdots & \\ \sin\theta_N & \cos\theta_N \end{bmatrix} \begin{pmatrix} u \\ v \end{pmatrix} = \begin{bmatrix} U_{r1} \\ U_{r2} \\ \vdots \\ U_{rN} \end{bmatrix}$$

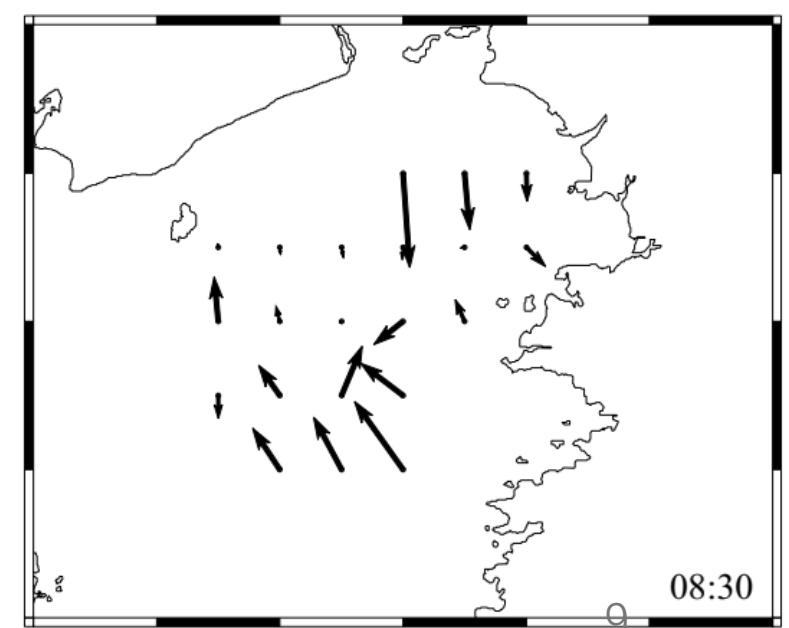
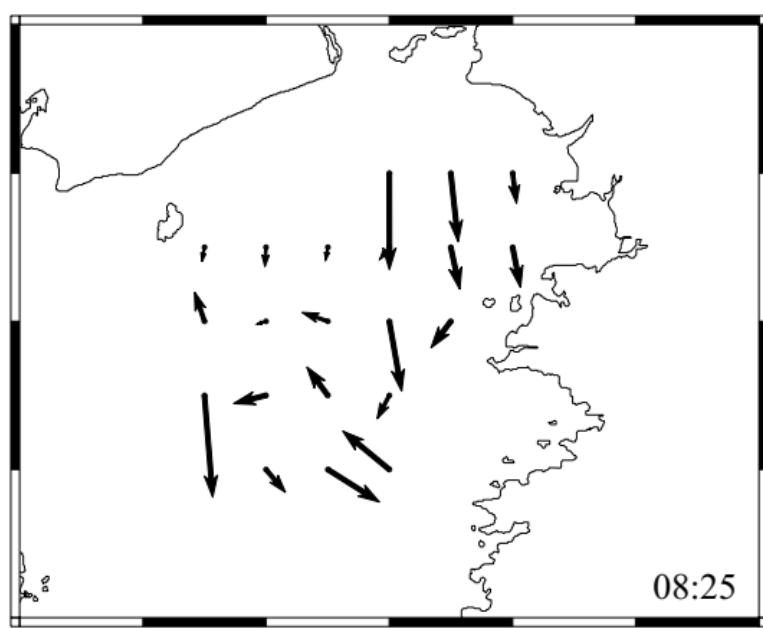
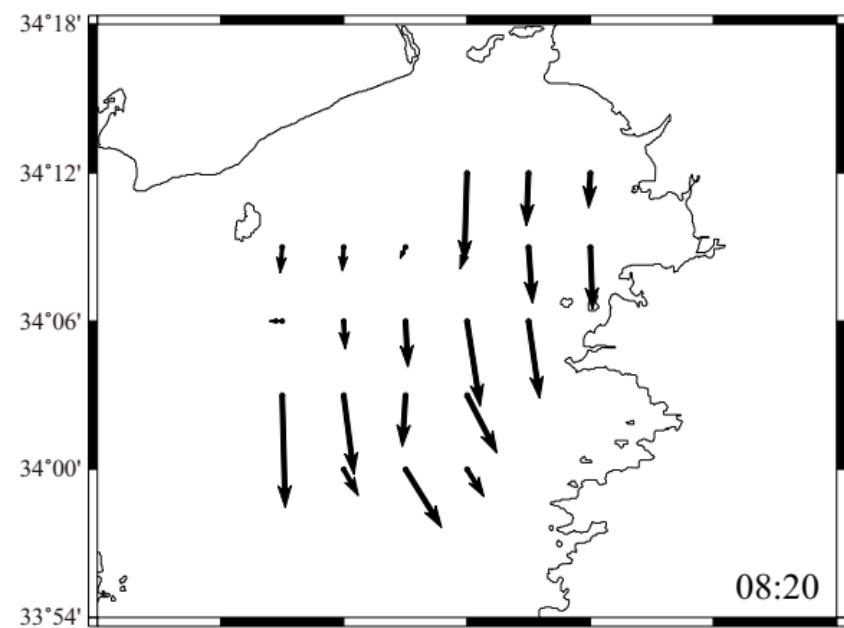
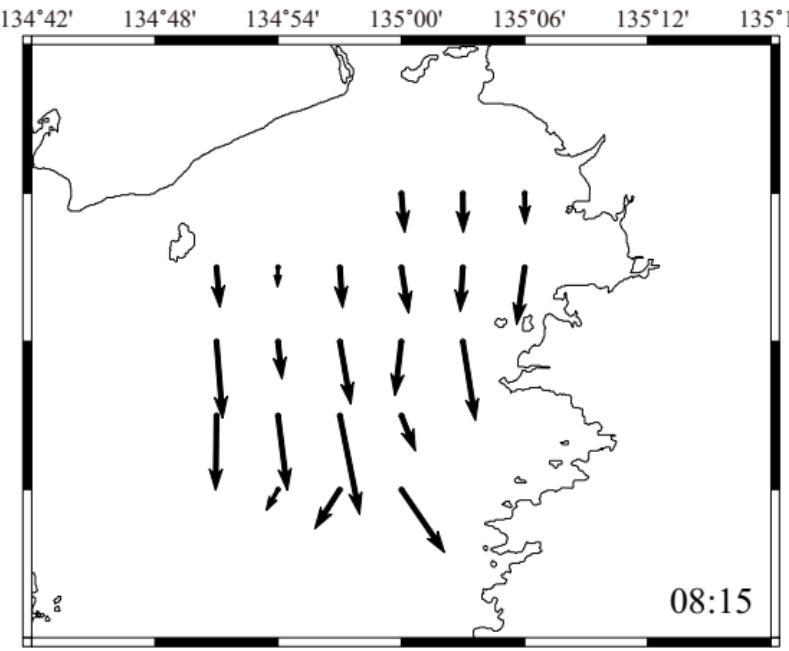
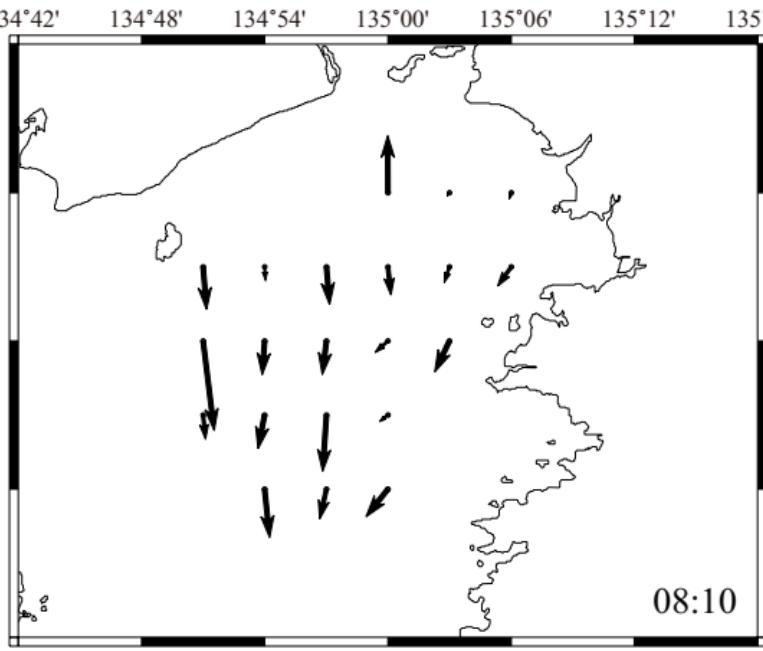
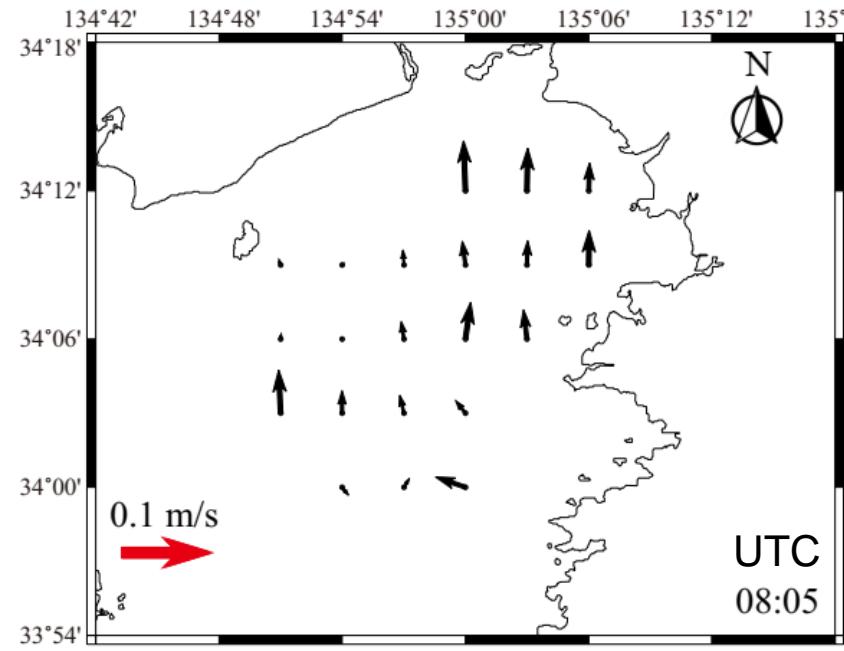
$i$ : Number of HF radar land station  
 $\theta_i$ : Azimuth of the grid  
 $U_{ri}$ : Velocity in the beam direction  
 $u, v$ : Velocity in the EW/NS direction

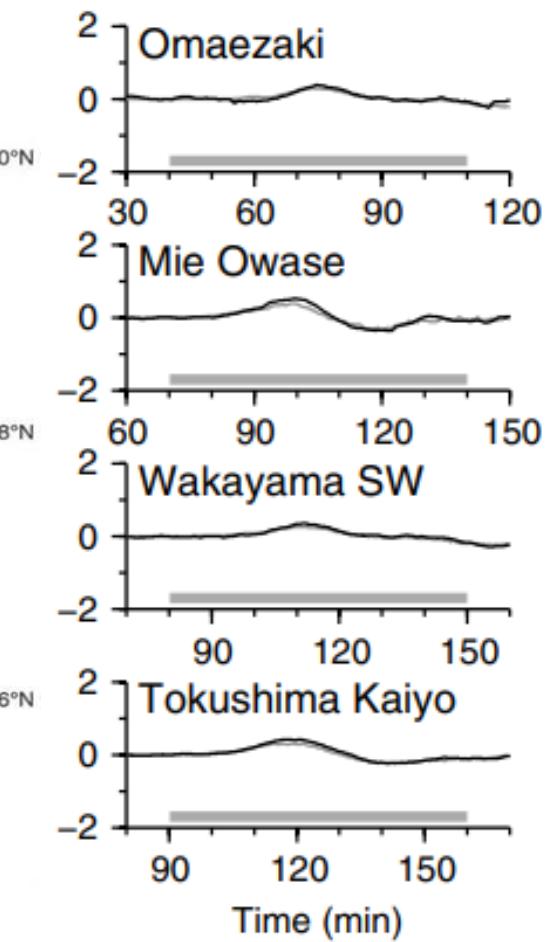
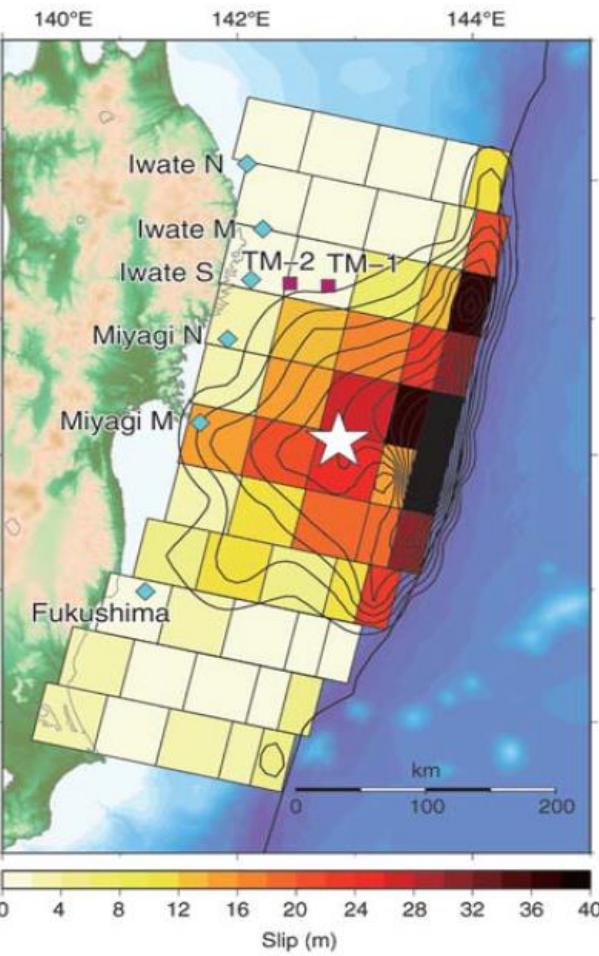
When  $N > 2$ :

$$\sum_{i=1}^N (U_{ri} - \hat{U}_{r1})^2 / \sigma_i^2 \rightarrow \min$$

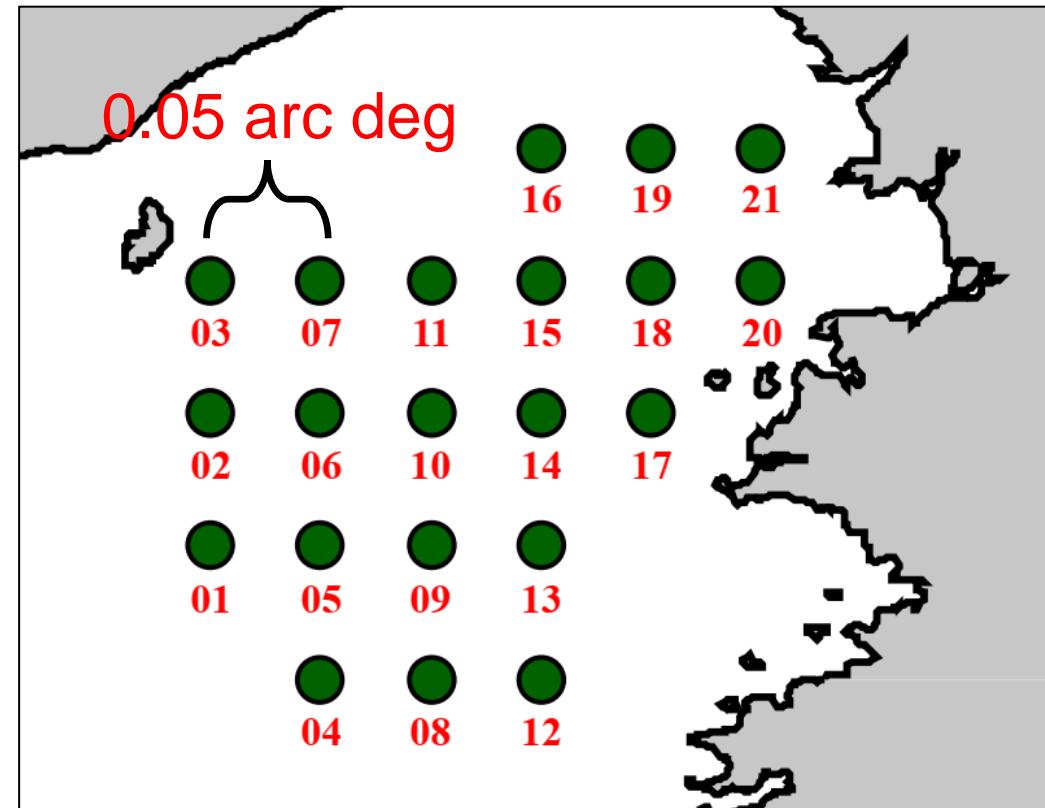
When  $N = 2$  (in this study):

$$\begin{pmatrix} u \\ v \end{pmatrix} = \begin{bmatrix} \sin\theta_1 & \cos\theta_1 \\ \sin\theta_2 & \cos\theta_2 \end{bmatrix}^{-1} \begin{bmatrix} U_{r1} \\ U_{r2} \end{bmatrix}$$





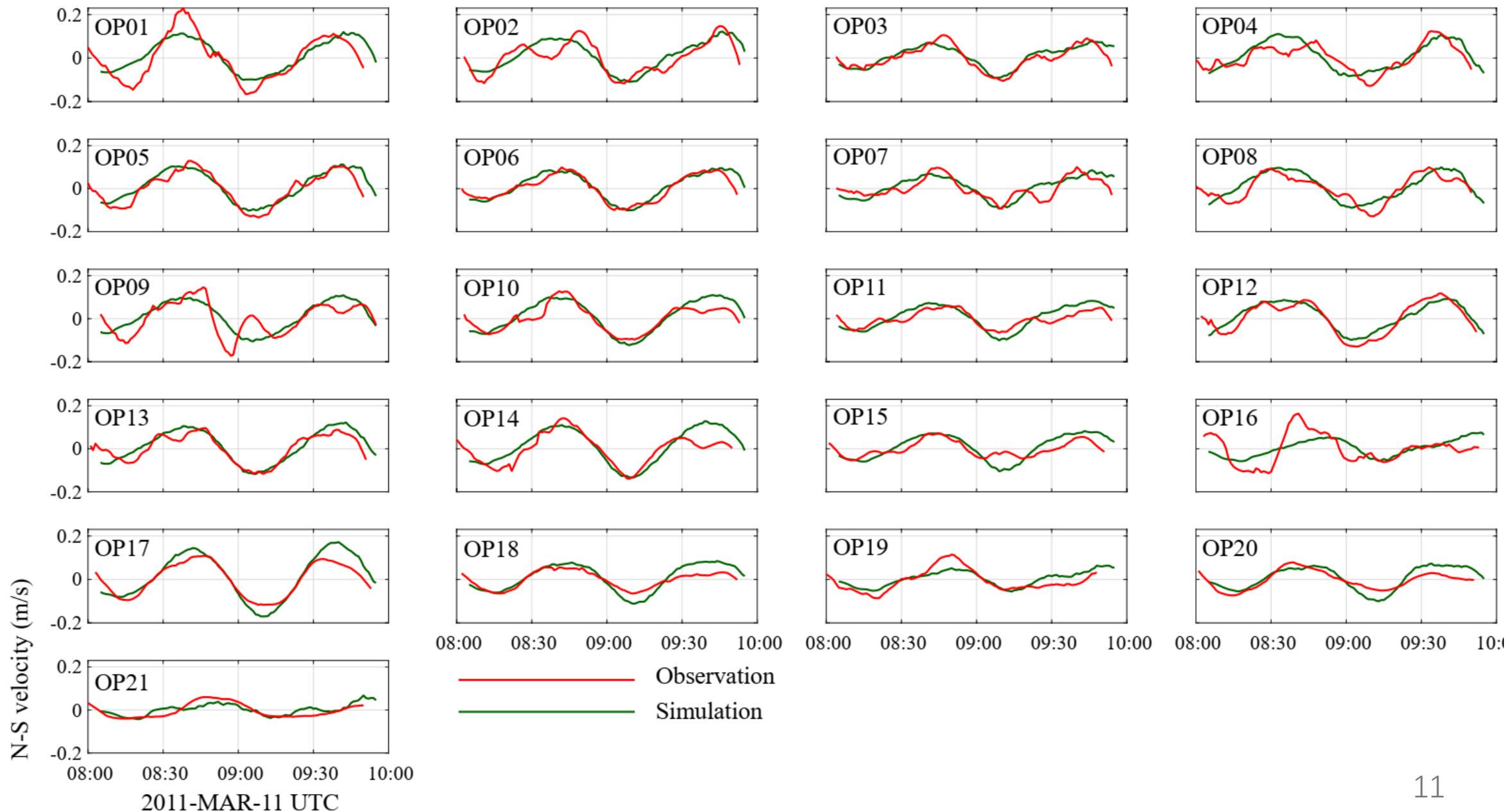
## Location of Observational Point (OP)



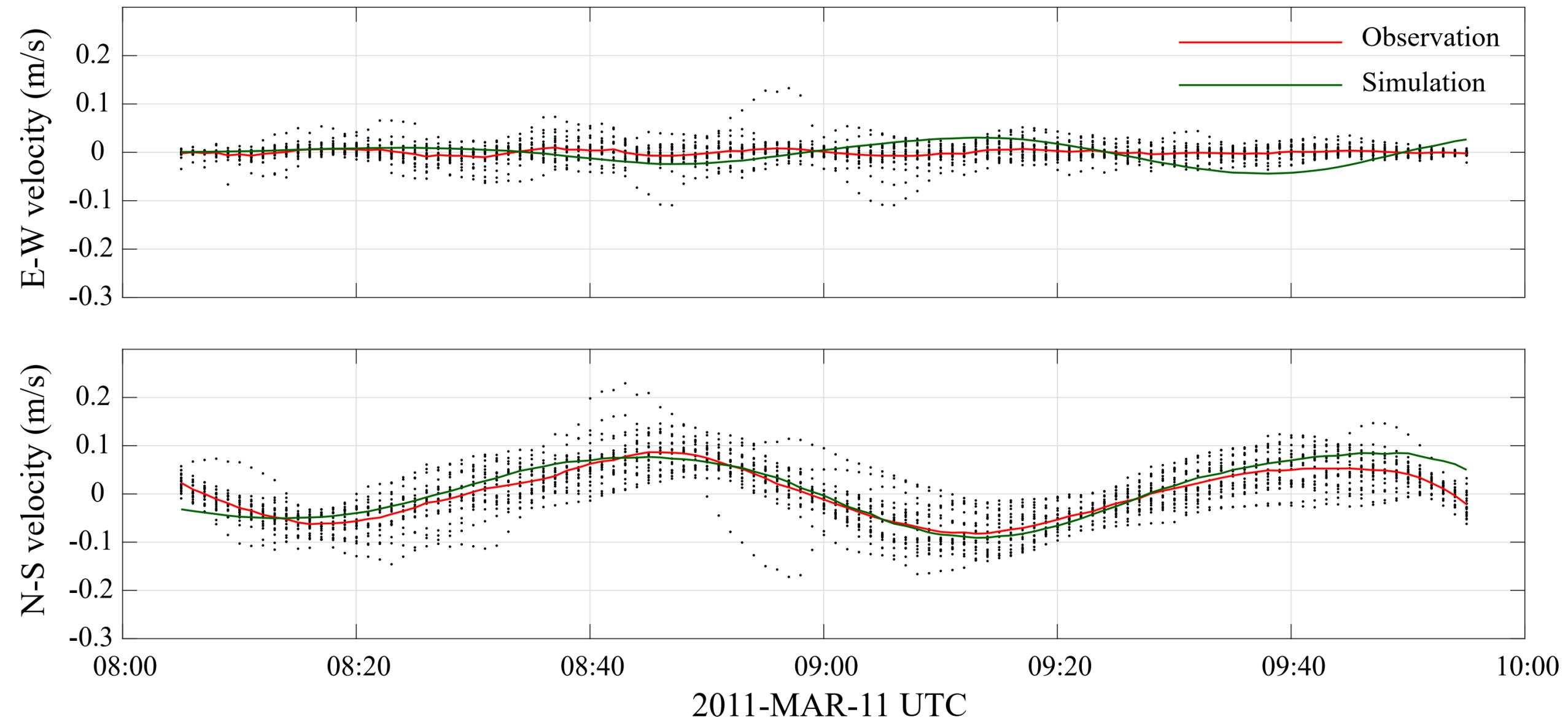
Satake et al. (2013)

- データ解析の正確性を確認するために、観測された流速とシミュレーション値を比較した。
- シミュレーション値は断層モデルによって計算され、検潮計の波形を正確に再現できることから、流速の再現においても正確であると仮定した。

# Time Series of Sea Surface Current

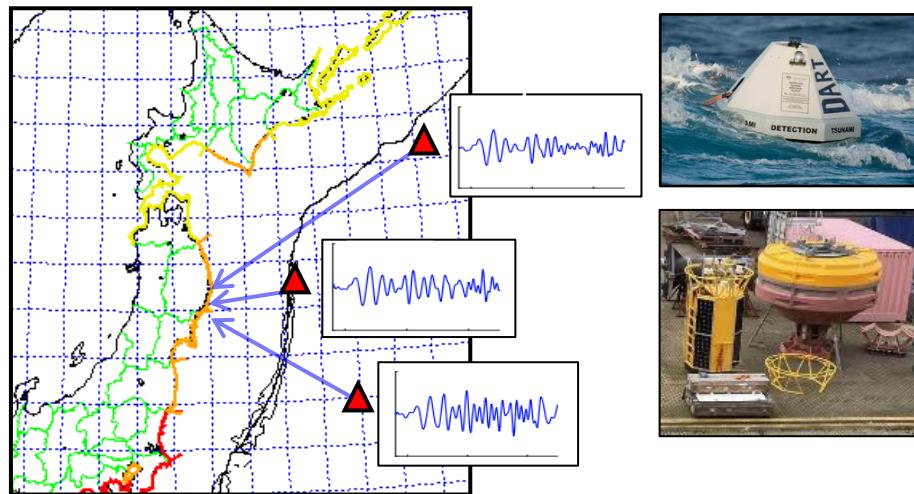


# Time Series of Sea Surface Current

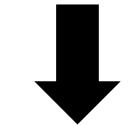


2011-MAR-11 UTC

# Data Assimilation for Early Warning

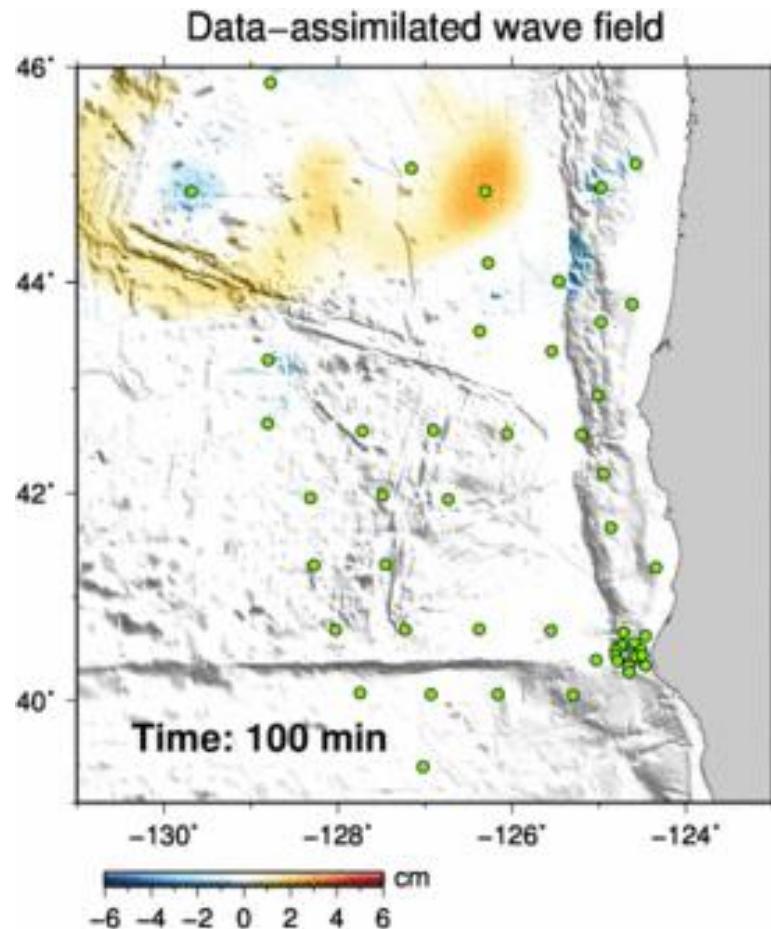


Offshore Tsunami  
Observation

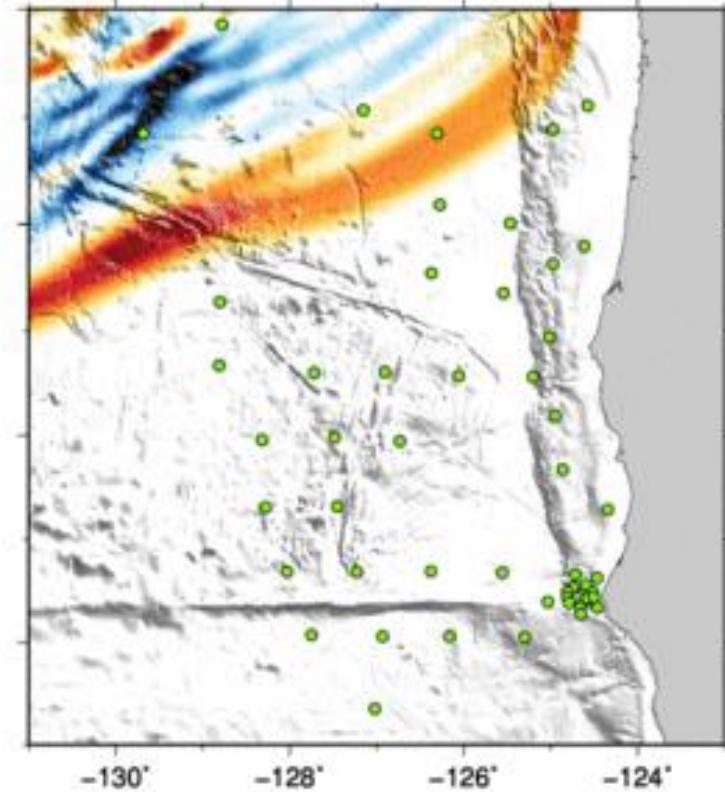


Tsunami Forecasting

Past study: 2012 Haida Gwaii tsunami (synthetic)



Wave field from slip distribution



*Do not need source information!*

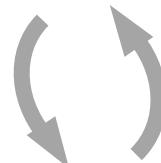
(Gusman et al., 2016)

Tsunami wavefield  $\boldsymbol{x}_n = (h(n\Delta t, x, y), P(n\Delta t, x, y), Q(n\Delta t, x, y))^T$

Height            X-Velocity            Y-Velocity

I. Forecasting Step

$$\boldsymbol{x}_n^f(h, P, Q) = F \boldsymbol{x}_{n-1}^a(h, P, Q)$$



II. Assimilating Step

$$\boldsymbol{x}_n^a(h, P, Q) = \boldsymbol{x}_n^f(h, P, Q) + \boldsymbol{W}(\mathbf{z}_n(\boldsymbol{P}, \boldsymbol{Q}) - \boldsymbol{H}\boldsymbol{x}_n^f(h, P, Q))$$

$\boldsymbol{x}_n^f$ : Forward tsunami wavefield

$\boldsymbol{x}_n^a$ : Assimilated tsunami wavefield

$F$ : Propagation matrix

$\boldsymbol{W}$ : Weight matrix\*\*

$H$ : Sparse linear observation matrix

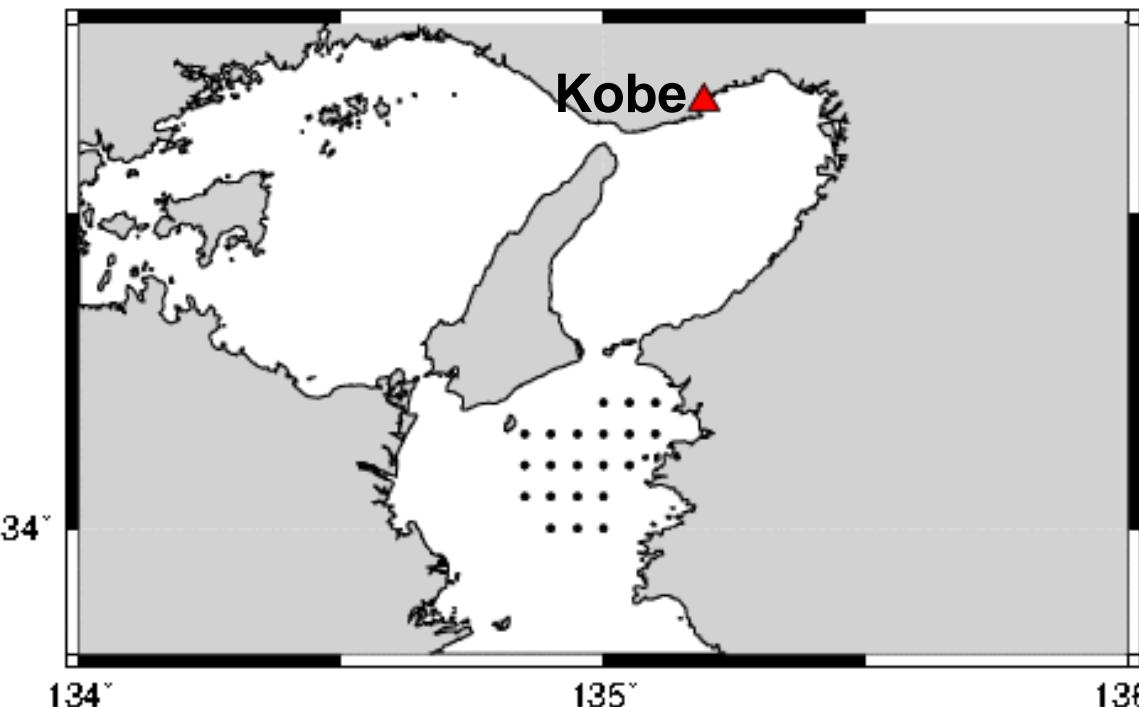
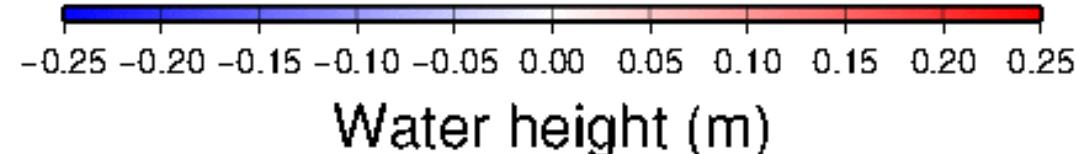
$\mathbf{z}_n$ : Observation of HF radar (velocity)

**Assimilation starts at 08:05 UTC (JST 17:05)**

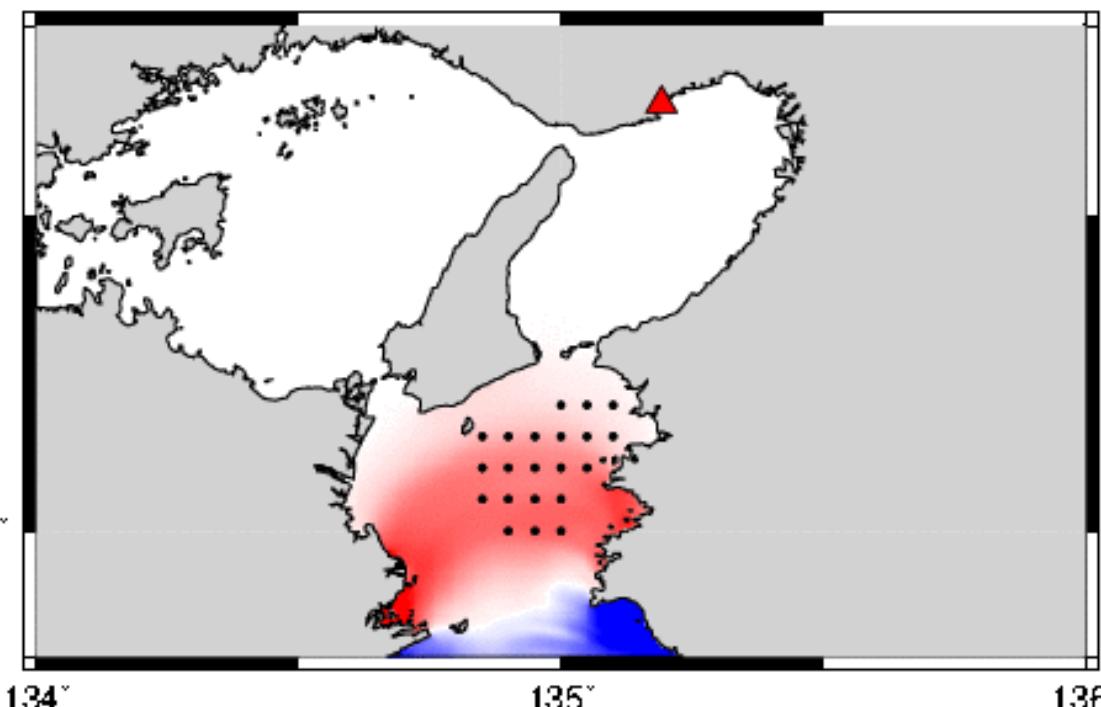
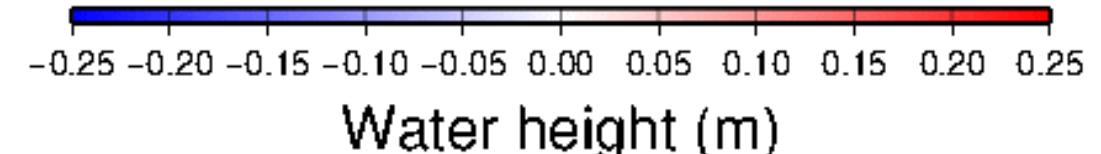
\*\* New algorithm of calculating  $\boldsymbol{W}$  was proposed by Dr. Sahana

### 3. 結果

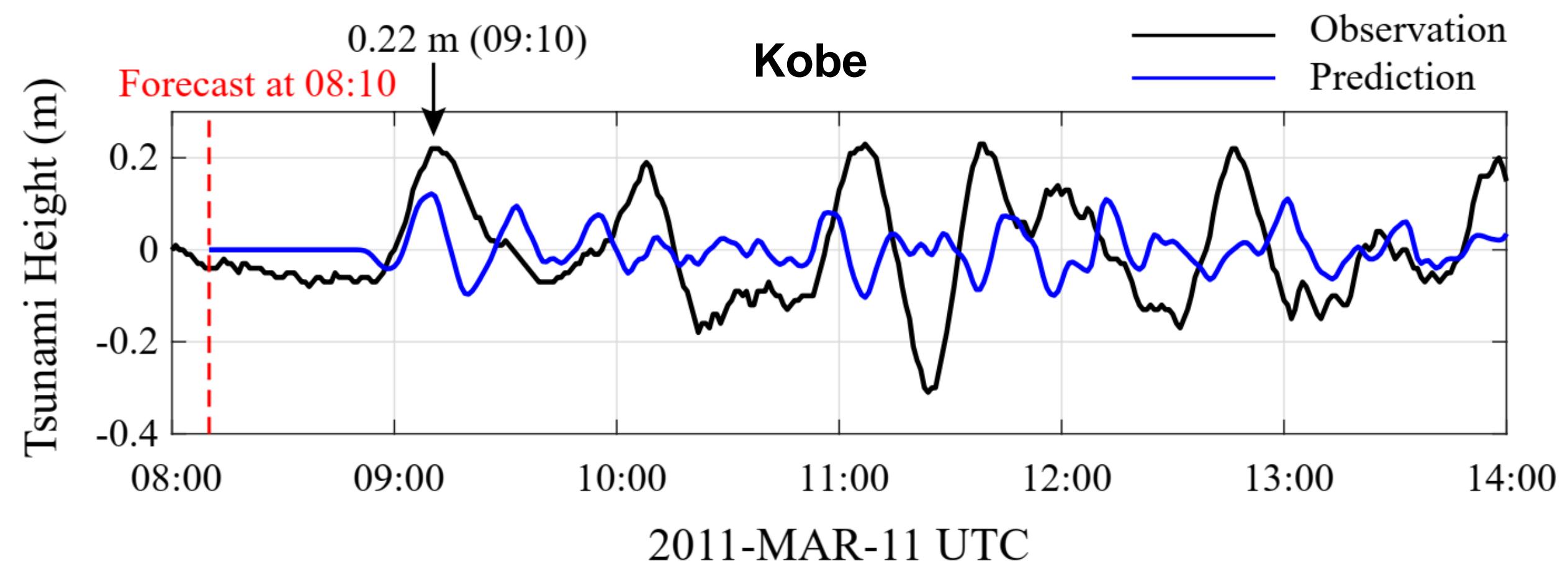
Time: 2011 March 11, 08:05 – 09:00 UTC (17:05 – 18:00 JST)



**Forecasted** tsunami wavefield using  
data assimilation of HF radar



**Simulated** tsunami wavefield computed  
from source model of Satake et al. (2013)



Observed maximum height: 0.23 m

Predicted maximum height: 0.12 m

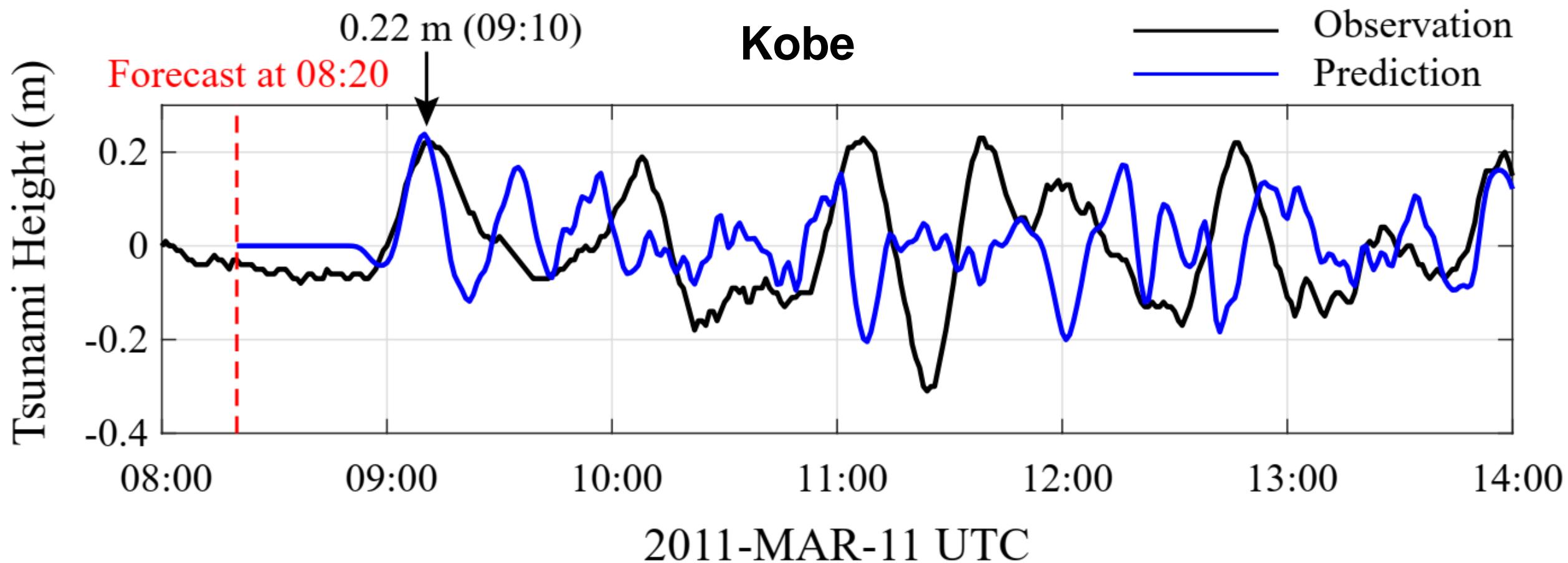
Accuracy (%): 52.2%

最大振幅：津波早期警報にとって大事

Normalized Prediction Error (Navarrete et al., 2019)

$$\min \left\{ \sqrt{\frac{\frac{1}{T} \sum_{t=1}^T (y_{pre}(t+L) - y_{obs}(t))^2}{\frac{1}{T} \sum_{t=1}^T (y_{pre}(t+L))^2 + \frac{1}{T} \sum_{t=1}^T (y_{obs}(t))^2}}; 1 \right\} = 0.991$$

後続波：津波警報解除にとって大事



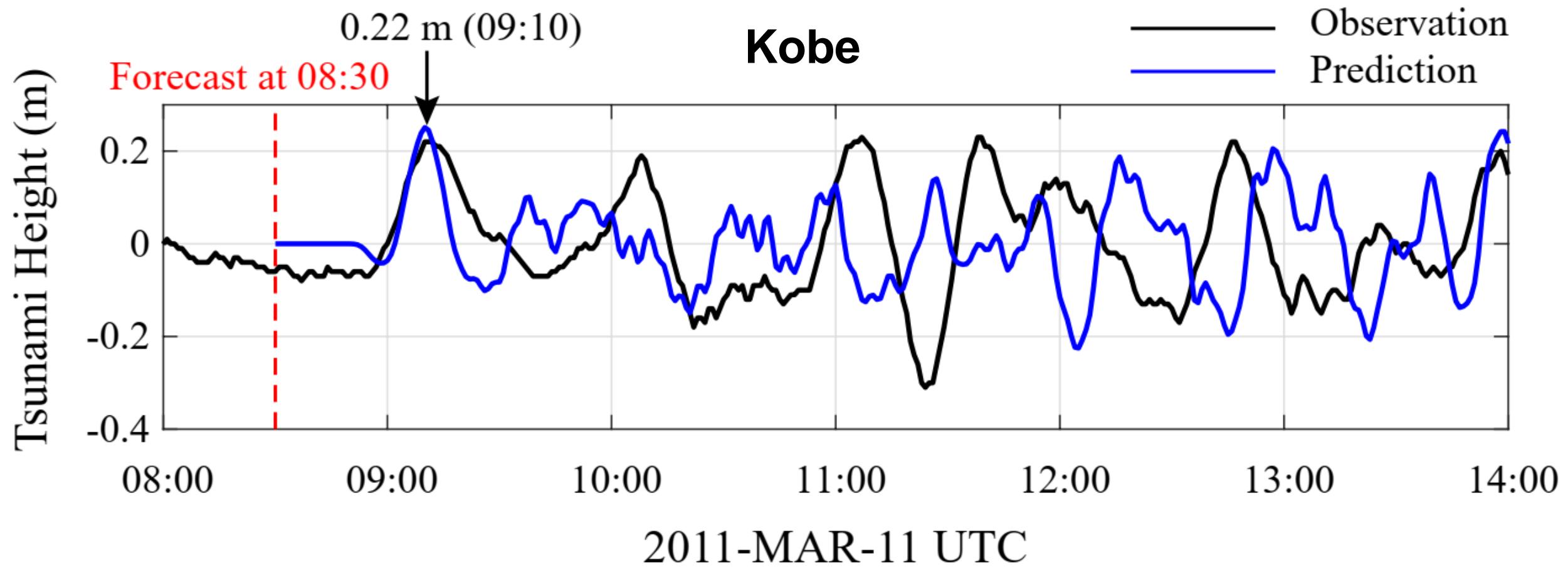
Observed maximum height: 0.23 m

Predicted maximum height: 0.24 m

Accuracy (%): 95.8%

Normalized Prediction Error

$$\min \left\{ \sqrt{\frac{\frac{1}{T} \sum_{t=1}^T (y_{pre}(t+L) - y_{obs}(t))^2}{\frac{1}{T} \sum_{t=1}^T (y_{pre}(t+L))^2 + \frac{1}{T} \sum_{t=1}^T (y_{obs}(t))^2}}; 1 \right\} = 0.976$$



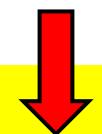
Observed maximum height: 0.23 m

Predicted maximum height: 0.25 m

Accuracy (%): 92.0%

Normalized Prediction Error

$$\min \left\{ \sqrt{\frac{\frac{1}{T} \sum_{t=1}^T (y_{pre}(t+L) - y_{obs}(t))^2}{\frac{1}{T} \sum_{t=1}^T (y_{pre}(t+L))^2 + \frac{1}{T} \sum_{t=1}^T (y_{obs}(t))^2}}; 1 \right\} = 0.929$$



## 4. まとめ

- HF radar observed the tsunami of the 2011 Tohoku earthquake, with a value of ~ 0.1 m/s at most observational points after 08:00 (UTC).
- Data assimilation of surface current velocity successfully predicted the tsunami waveforms of Kobe tide gauge at 08:20, approximately 50 min prior to tsunami arrival.
- The normalized prediction error decreased over assimilation time.

**Thank you for your attention!**

### Article Navigation

RESEARCH ARTICLE | OCTOBER 22, 2024

✉ Early Publication

Tsunami Early Warning Using High-Frequency Ocean Radar System in the Kii Channel, Japan 

Yuchen Wang ; Kentaro Imai; Hiroki Horikawa

+ Author and Article Information

Seismological Research Letters (2024) | <https://doi.org/10.1785/0220240168> | Article history 

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